Compression of image using multi-wavelet techniques

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(Communicated by Madjid Eshaghi Gordji)

Abstract

Digital compression of images is a topic that has appeared in a lot of studies over the past decade to this day. As wavelet transform algorithms advance and procedures of quantization have helped to bypass current compression of image standards such as the JPEG algorithm. To get the highest effectiveness in compression of image transforms of wavelet need filters which gather a desirable character’s number i.e., symmetry and orthogonally. Nevertheless, wave design capabilities are restricted due to their ability to have all of such desirable characters at the same time. The multi-wavelet technology removes a few of the restrictions of the wavelet play more than the options of design and thus able to gather all desired Characters of transforming. Wavelet and multi-wave filter banks are tested on a larger scale with images, providing more useful analysis. Multiple waves indicate energy-compression efficiency (a higher compression ratio usually indicates a higher mean square error, MSE, in the compressed image). Filter bank Characters such as orthogonal and compact support, symmetry, and phase response are important factors that also affect MSE and professed quality of the image. The current work analyzes the multi-wave Characters effect on the performance of compression of images. Four multi-wavelength Characters (GHM, CL, ORT4) were used in this thesis and the compression of image performance of grayscale images was compared with common scalar waves (D4). SPIHT quantification device in stress chart and use of PSNR and subjective quality measures to assess performance. The results in this paper point out those multi wave characteristics that are most important for the compression of images. Moreover, PSNR results and subjective quality show

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Received: October 2021  Accepted: November 2021
similar performance to the best scalar and multi-waves. The analysis also shows that a programmer based on multi-band conversion significantly improves the perceived image quality.

Keywords: Image Processing, Compression, SPIHT, Multi-wavelet, MSE.

1. Introduction

Compression of image is a data compression type implemented to images as digital to minimize their size during transmission or storage. Algorithms that use the perception as visual and image statistical Characters of data mostly offer results being superior when compared with procedures of normal compression [22].

Schemes of transformation-based compression of image first participates converting spatial data to other field. Because the transformation goal is a compact and complete image representation, the decorative transformation must relate the distributed spatially energy to less samples of data without losing any data. Transformations as orthogonal are characterized by redundancy elimination in the image that transformed. Compression takes place in the step second if converted image is quantified as data with negligible power levels is overlooked [21].

Multiple waves have many advantages compared to scalar waves. Characters i.e., compressed orthogonally, support, symmetry, and high-order fading moments are well-known to be significant in processing of signal. A scalar wave cannot have all of these Characters at the same time but it can have multiple waves. Goodman, Li and Tang began a multi-wave study. Discover T[3] characterization of wavelet scaling functions. Hong and Wu [18] built a multivalve class with multiples of 4 and support [0, 2]. In general, after the introduction of the pre-filter technology, the 2-wave polymorphism can be successfully applied in a compression of image application.

In this paper, we’ll look at four new build-action filters from Multi-wavelet for compression of image. So we present some simple formulas for creating high and low pass filters. Therefore, the technology of pre-filtering must be introduced to obtain a good frequency fusing characteristic of the filter of matrix with the pre-filter. For evaluating the multi-wave effectiveness of coding of low bit-rate image, efficient SPIHT encoding for multi-band transactions was achieved [11], and accomplished using an appropriate scanning strategy across scales and within each detailed sub band [12].

2. Research Stages

The suggested system was designed to get a better compression of image visual quality. There are two visual quality measurements that are used: PSNR, and MSE. The main function of the suggested system was compressed the bitmap image to a compressed image by using the (BMP file formats).

In our suggested system, we suggest the four multi-wavelet filters to increase the compression ratio with the best PSNR and MSE values. Also, the wavelet filter (D4) is used for comparing the results of the multi-wavelet with the wavelet results. The prefilters are used in the preprocessing operation before the decomposed operation stage [13, 14]. The suggested system is called Compression of image using Multi-wavelet System (ICUMWT). ICUMWT divided into the following diagram of the suggested system is displayed in Figure [1].
2.1. Image Loadings

This suggested part system was planned to image loading into the suggested system buffer and displays them in the viewer areas. The suggested system was designed to deal with BMP file format. The suggested system will begin operation of loading through showing the open dialog for making users to choice the file of image. This image shall be read from the disk in memory to a buffer temp \[5, 2\]. The algorithm (1.1) of such part is:

**Algorithm (1.1) Image loading**

<table>
<thead>
<tr>
<th>Step 1: Displaying dialog as open.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Step 2: Loading the images into the memory.</td>
</tr>
<tr>
<td>Step 3: Display image in the suggested system viewer.</td>
</tr>
<tr>
<td>Step 4: End.</td>
</tr>
</tbody>
</table>

2.2. Pre-Calculations

After loading the image the suggested system prepare to operate the multi-wavelet perfiltering\[7\]. This function of suggested system was used in the compression of image by using the multi-wavelet only. No prefilters were used in the scalar wavelet. The prefilters are used in the prefiltering function.
are called Interpolation prefilters with following filter matrix values:

\[
Q_0 = \begin{bmatrix}
\frac{3}{8\sqrt{6}} & \frac{5}{8\sqrt{6}} \\
0 & 0
\end{bmatrix}
\]  \hspace{1cm} (2.1)

\[
Q_1 = \begin{bmatrix}
\frac{3}{8\sqrt{6}} & 0 \\
0 & \frac{1}{\sqrt{13}}
\end{bmatrix}
\]  \hspace{1cm} (2.2)

These prefilters are selected by the practical experimental for getting best values of the PSNR and MSE of the compressed image by using the multi-wavelet filters. The algorithm (1.2) of this function is shown as [9]:

<table>
<thead>
<tr>
<th>Algorithm (1.2) Prefiltering</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input:</strong> loaded image with prefilters values.</td>
</tr>
<tr>
<td><strong>Output:</strong> Filtered image.</td>
</tr>
<tr>
<td><strong>Step 1:</strong> Read image arrays.</td>
</tr>
<tr>
<td><strong>Step 2:</strong> Convolve the image with the prefilters values using equation (2.1), (2.2).</td>
</tr>
<tr>
<td><strong>Step 3:</strong> Save the result image.</td>
</tr>
<tr>
<td><strong>Step 4:</strong> End.</td>
</tr>
</tbody>
</table>

2.3. Image Decomposition using Multi-wavelet

The multi-wavelet transform of separable 2-D is done as transform of 1-D row followed by a transform of 1-D column. Figure 2 displays the multi-wavelet filter bank for single decomposition of level 2-D. The 16 sub-bands produced following the transformations of column and row are showed in Figure 2. Befor encoding along with SPIHT, the sub-bands are set as displayed in Figure 3 (The sub-bands are signified via XiYj in which, X, Y = L, H; L and H corresponding to low and high passes outputs, correspondingly. The sub-scripts i, j = 0, 1 corresponding to the filters in branch Y or X). A method of restoring the dependencies aspatial is elaborated in the coming sub-sections. Regarding multi-wavelets, decomposition of one-level displays that a large similarity amount presents in the blocks of $2 \times 2$ which comprising the $L_iH_j$, $H_iL_j$ and $H_iH_j$ sub-bands. For restoring the dependencies as spatial, we were interleaving the high sub-bands frequency $XiYj$ ($XiYj = L_iL_j$) into $XY$ as single block. Therefore, blocks HL, LH, and HH are produced, and the algorithm (1.3) of the image decomposition show as [8].

Figure 2: The 2-D Multi-wavelet filter Bank.
Compression of image using multi-wavelet techniques

<table>
<thead>
<tr>
<th>$L_0 L_0$</th>
<th>$L_1 L_0$</th>
<th>$L_0 H_0$</th>
<th>$L_1 H_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_0 L_1$</td>
<td>$L_1 L_1$</td>
<td>$L_0 H_1$</td>
<td>$L_1 H_1$</td>
</tr>
<tr>
<td>$H_0 L_0$</td>
<td>$H_1 L_0$</td>
<td>$H_0 H_0$</td>
<td>$H_1 H_0$</td>
</tr>
<tr>
<td>$H_0 L_1$</td>
<td>$H_1 L_0$</td>
<td>$H_0 H_1$</td>
<td>$H_1 H_1$</td>
</tr>
</tbody>
</table>

Figure 3: Single-level multi-wavelet decomposition showing 16 sub-bands.

**Algorithm (1.3) Multi-wavelet Decomposition**

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Convolve the lowpass filters with rows and save the results.</td>
</tr>
<tr>
<td>2</td>
<td>Convolve the lowpass filters with the columns (of the result from step 1) and sub-sumable this result by taking every other values; this offers us the lowpass-lowpass (LL) sub image.</td>
</tr>
<tr>
<td>3</td>
<td>From step 1, convolving the result, lowpassing filtered rows, with the high pass filter for columns via taking each other value to produce the sub-image lowpass-highpass (LH).</td>
</tr>
<tr>
<td>4</td>
<td>Convolving the image as original with the filters of Highpass on rows and saving the results.</td>
</tr>
<tr>
<td>5</td>
<td>From step 4, convolving the results on the columns with the filter of lowpass; sub samples to produce the sub-image of highpass-lowpass (HL).</td>
</tr>
<tr>
<td>6</td>
<td>For obtaining the sub-image as highpass-highpass (HH), convolving the columns of the results from step 4 along highpass filter.</td>
</tr>
<tr>
<td>7</td>
<td>Return to step 1.</td>
</tr>
<tr>
<td>8</td>
<td>End.</td>
</tr>
</tbody>
</table>

**2.4. Compression of image Wavelet Transform**

In this function, the suggested system will start compression of image using the wavelet transform technique. This function depends on the wavelet decomposition using D4 filter, the filter coefficients show in equations (2.3) and (2.4). The result of the decomposition operation will send to the quantization operation [19]. Final result from the quantization operation will send to the coding operation. The compressed image will saved into the file. The reverse operations will apply to the compressed image to reconstruct the image. Then the suggested system will calculate the quality measurements (PSNR and MSE). The algorithm (1.4) of this function is shown as [15]:

$$H = \begin{bmatrix} 1+\sqrt{3} \ 3+\sqrt{3} \\ 4\sqrt{2} \ 4\sqrt{2} \end{bmatrix}$$ \hspace{1cm} (2.3)

$$G = \begin{bmatrix} 1-\sqrt{3} \ 3-\sqrt{3} \\ 4\sqrt{2} \ 4\sqrt{2} \end{bmatrix}$$ \hspace{1cm} (2.4)
Algorithm (1.4) Wavelet Compression of image

Output: Compressed Image.
Step 1: Load image file.
Step 2: Do wavelet decomposition technique on the image, using filter coefficients (equations (2.3) and (2.4)).
Step 3: Apply the quantization algorithm.
Step 4: Apply the coding algorithm.
Step 5: Save the compressed Image.
Step 6: Apply the ICoding algorithm.
Step 7: Apply the IQuantization algorithm.
Step 8: Apply Reconstruction algorithm.
Step 9: Calculate the PSNR and MSE value.
Step 10: Display results.
Step 11: End.

2.5. Compression of image Using Multi-wavelet

In our suggested system, there are four filters of Multi-wavelet are used to compressed images. These filters used to display the differences of effects the Multi-wavelet compression on the images. Before starting the convolve the Multi-wavelet filters, the preprocessing operation must be done before applying the Multi-wavelet filter on the image [20].

In our suggested system, the preprocessing filter is used to apply the preprocessing and postprocessing operation [4]. The algorithm (1.5) of the preprocessing is shown as:

Algorithm (1.5) Multi-wavelet Compression of image

Input: Image File.
Output: Preprocessing image.
Step 1: Load the image file using the image Loading algorithm.
Step 2: Apply the equation (2.3) and equation (2.4) on the image rows and columns.
Step 3: Save the result into the temp file.
Step 4: Display the results.
Step 5: End.

2.5.1. The GHM Filter Compression Procedures

The G as highpass filter and H as lowpass filter in the multi-wavelet filter bank are matrices of $2 \times 2$. Therefore, they require to be convolved with 2 data rows.

Nevertheless, for signals of 1-D, we offer just one data row; thus we must pre-processing the signal of 1-D to get 2 data rows. The pre-processing must not destroy bases symmetry and/or orthogonality. A solution to such issue is simply input repeating. However, such solution is equel to over-sampling and results in technique are expansive which is not fit for compression [3].

Similarly to a scalar bank filter, the branches of lowpass in a filter bank as multi-wavelet must keep some inputs as polynomial whereas the branches of highpass must annihilate them completely [6]. The multi-wavelet annihilation character of the filter bank relies on its order of approximation. This is the first method was used to compressed the image file (gray-level). The algorithm (1.6) of this method is as shown below:
Algorithm (1.6) The GHM Method

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Load the preprocessing image file using the image Loading algorithm.</td>
</tr>
<tr>
<td>2</td>
<td>Apply equations (3.22) and (3.23) on the image rows and columns.</td>
</tr>
<tr>
<td>3</td>
<td>Apply the quantization algorithm.</td>
</tr>
<tr>
<td>4</td>
<td>Apply the coding algorithm.</td>
</tr>
<tr>
<td>5</td>
<td>Save the compressed Image.</td>
</tr>
<tr>
<td>6</td>
<td>Apply the ICoding algorithm.</td>
</tr>
<tr>
<td>7</td>
<td>Apply the IQuantization algorithm.</td>
</tr>
<tr>
<td>8</td>
<td>Apply equation (3.22) and (3.23) on the image rows and columns for reconstruct the image.</td>
</tr>
<tr>
<td>9</td>
<td>Calculate the PSNR and MSE values.</td>
</tr>
<tr>
<td>10</td>
<td>Calculate Compression Ratio value.</td>
</tr>
<tr>
<td>11</td>
<td>Display results.</td>
</tr>
<tr>
<td>12</td>
<td>End.</td>
</tr>
</tbody>
</table>

2.5.2. CL Filter Compression Method

Another symmetric orthogonal example of multi-wavelets with order 2 approximation is in due to Chui and Lain (CL). They’re both functions of scaling are reinforced on \([0, 2]\), that is longer slightly than GHM. For the system of (CL), just 3 H matrices and 3 G matrices are needed. Here \(a_0 = 1/2\sqrt{2} \text{ and } a_2 = 1/4\sqrt{2}\), CL scaling and wavelet functions are less smooth than GHM once.

\[
H_0 = a_1 \begin{bmatrix} 1 & -1 \\ \sqrt{2} & -\sqrt{2} \end{bmatrix},
H_1 = a_1 \begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix},
H_2 = a_1 \begin{bmatrix} \frac{1}{2} & \frac{1}{\sqrt{7}} \\ -\frac{1}{\sqrt{7}} & \frac{1}{2} \end{bmatrix}
\]

Reconstructed Image (2.5)

\[
G_0 = a_2 \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix},
G_1 = a_2 \begin{bmatrix} -4 & 0 \\ 0 & 2\sqrt{7} \end{bmatrix},
G_2 = a_2 \begin{bmatrix} 2 & 2 \\ 1 & 1 \end{bmatrix}
\]

Postfilters Operations (2.6)

Algorithm (1.7) The CL Method

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Load the preprocessing image file using the image Loading algorithm.</td>
</tr>
<tr>
<td>2</td>
<td>Apply equations (2.5) and (2.6) on the image rows and columns.</td>
</tr>
<tr>
<td>3</td>
<td>Apply the quantization algorithm.</td>
</tr>
<tr>
<td>4</td>
<td>Apply the coding algorithm.</td>
</tr>
<tr>
<td>5</td>
<td>Save the compressed Image.</td>
</tr>
<tr>
<td>6</td>
<td>Apply the ICoding algorithm.</td>
</tr>
<tr>
<td>7</td>
<td>Apply the IQuantization algorithm.</td>
</tr>
<tr>
<td>8</td>
<td>Apply equations (2.5) and (2.6) on the image rows and columns for reconstruct the image.</td>
</tr>
<tr>
<td>9</td>
<td>Calculate the PSNR and MSE values.</td>
</tr>
<tr>
<td>10</td>
<td>Calculate Compression Ratio value.</td>
</tr>
<tr>
<td>11</td>
<td>Display results.</td>
</tr>
<tr>
<td>12</td>
<td>End.</td>
</tr>
</tbody>
</table>
2.5.3. ORT4 Filter Compression Method

The determined symmetric pair by 3coefficients is another beneficial system of orthogonal multi-wavelet with approximation of 2nd order [17]. The Low pass and high pass filters coefficients show in equation (2.7) and equation (2.8).

\[
H_0 = \begin{bmatrix} 0 & \sqrt{2+\sqrt{2}} \\ 0 & \sqrt{2-\sqrt{2}} \end{bmatrix}, H_1 = \begin{bmatrix} 3/4 & 1/4 \\ 1/4 & \sqrt{2} 2\sqrt{2} \end{bmatrix}, H_2 = \begin{bmatrix} 2-\sqrt{7} 2\sqrt{2} \\ \sqrt{2+\sqrt{2}} 4 \end{bmatrix} \quad (2.7)
\]

\[
G_0 = \begin{bmatrix} 1/2 & -1/2 \\ \sqrt{7}/4 & -\sqrt{7}/4 \end{bmatrix}, G_1 = \begin{bmatrix} 2 & 0 \\ 0 & \sqrt{7} 2\sqrt{2} \end{bmatrix}, G_2 = \begin{bmatrix} 1/2 & 1/2\sqrt{2} \\ -\sqrt{7}/4 & -\sqrt{7}/4 \end{bmatrix} \quad (2.8)
\]

Algorithm (1.8) The ORT4 Method

Input: Preprocessing Image File.
Output: Compressed image.

Step 1: Load the preprocessing image file using the image Loading algorithm.
Step 2: Apply equations (2.7) and (2.8) on the image rows and columns.
Step 3: Apply the quantization algorithm.
Step 4: Apply the coding algorithm.
Step 5: Save the compressed Image.
Step 6: Apply the ICoding algorithm.
Step 7: Apply the IQuantization algorithm.
Step 8: Apply equations (2.7) and (2.8) on the image rows and columns for reconstruct the image.
Step 9: Calculate the PSNR and MSE values.
Step 10: Calculate Compression Ratio value.
Step 11: Display results.
Step 12: End.

2.5.4. Image Quantization Algorithm

The method of quantization utilized to produce all the results in the current work is the quantizer of SPIHT. It is an embedding coder which is refining the thoughts existed in embedded (EZW) coder as zero-tree wavelet. SPIHT and EZW [23] attain good effectiveness through exploiting the spatial pixels dependencies in diverse wavelet transform sub-bands. The coder of SPIHT was selected for the trials in the current work because of its good performance as computational and objective.

In the SPIHT quantization scalar algorithm, origination at the coarsest resolution, the coefficients are examined versus a threshold. Compression is attained via single assigning a bit to a whatever set where all members are under the threshold (in-significant). The threshold is detected as [1][23]:

\[
T_p = \frac{C_{\text{max}}}{2p + 1} \quad (2.9)
\]

In which \( p = 0, 1, \ldots, \) of \( p \) as the pass index and

\[
C_{\text{max}} = 2\lceil \log_2 \max |C_{i,j}| \rceil \quad (2.10)
\]

In which \( C_{i,j} \) is the coefficient in the image at coordinate \((i, j)\). For whichever coefficient, a significance exam is done as that.
Basically, the threshold is \( \frac{1}{2} \) the biggest integer 2 powers which go beyond the maximum coefficient value of grey-scale, in few images there are some coefficients in the pass as initial which go beyond such threshold.

When in a set just, there is one coefficient go beyond the threshold in whichever set, it still would need complete significance bit-map transmission for such set for identifying such coefficient. For determining if that is possible, the simple exam \( (C_{\text{max}} < 3T_0/2) \) is presented. When the exam is contented, then a minimized threshold for pass 0 is presumed \([16]\), as:

\[
S_p(C_{i,j}) = \begin{cases} 
1, & \text{max} |C_{i,j}| \geq T_p \\
0, & \text{Otherwise}
\end{cases}
\] (2.11)

For such coefficients which become significantly new in the early pass, a bit is utilized to specify whether such coefficients also would go beyond the \( T_0 \) threshold from formula (2.11) that previously would have been implemented. The bits that extra transmitted are traded-off versus not transmitting some bit-maps, as an effectively consequence of merging 2 passes. In all compressed images via the scheme being modified, declining in bit-rate happened. Some latency transmission will take place, and 3 extra exams are needed in the algorithm being modified for checking if the algorithm is in its pass as initial.

3. Image Coding Algorithm

The algorithm of SPIHT contains 3 stages: initialization, sorting, and refinement. It is sorting the coefficients of wavelet in 3 lists of order: the insignificant sets list (LIS), the insignificant pixels list (LIP), and the significant pixels list (LSP). At the initialization SPIHT algorithm stage, the 1st describes a start threshold because of the maximum value in the coefficients of wavelet pyramid, then groups the LSP as list being empty and places all coefficients coordinates in the coarsest wavelet pyramid level (such as the lowest band of frequency; LL band) into the LIP and such that have also descendants into LIS. The pixels in the coarsest pyramid level are assembled into blocks adjacent pixels, and in every block one of no descendants. For sorting pass, the algorithm 1st is sorting the LIP elements and then the sets of roots in the LIS. For every pixel in the LIP, it executes an importance exam versus the present threshold and outputs the test result to the output bitstream.

All results of test are coded as either 1 or 0, based on the exam outcome, thus the SPIHT algorithm produces directly bitstream as binary. When a coefficient is noteworthy, its symbol is encoded and then its coordinate is moving to the LSP.

Throughout the sorting of LIS pass, the encoder of SPIHT perform the important exam for every set in the LIS and outputs the significance data. When a set is important, it is separated into its leaves and offspring. Partitioning and sorting are done till all important coefficients have been detected and stored in the LSP. Following all elements sorting pass, in the LIS and LIP, SPIHT carries out a refinement pass with the existing threshold in the LSP for all entries, excluding such that were moved to the LSP throughout the last sorting pass. Then, the existing threshold is divided via 2 and the stages of refinement and sorting are persistent till exhaustion of predefined bit-budget.

For the coming, we 1st describe the symbols and sets necessary for SPIHT, and then we are listing the whole algorithm of SPIHT coding.

Definitions

A. \( C (I, j) \): transformed wavelet coefficient at coordinate \((I, j)\).
B. $O(I,j)$: coordinates set of all node offspring $(I,j)$.

C. $D(I,j)$: coordinates set of all node descendants $(I,j)$.

D. $L(I,j)$: coordinates set of all node leaves $(I,j)$, $L(I,j) = D(I,j) - O(I,j)$.

E. $H$: coordinates set of all nodes in the level as coarsest of coefficients wavelet pyramid.

F. $S_n(I,j)$: coordinate set significance test $f(I,j)$ at bit plane level $n$

$$S_{n(i,j)} = \begin{cases} 1 & \text{If} \ max_{i,j} |C_{i,j}| \geq 2^n, \\ 0 & \text{Otherwise} \end{cases}$$

G. Sets of type A: for type A sets, the significance exams are to be implemented to all descendants $D(I,j)$.

H. Sets of type B: for type B sets, the significance exam are to be implemented just to the leaves $L(I,j)$.

I. $n_{max}$: maximum bit plane level required for coding

$$n_{max} = \lfloor \log_2 \{ \max_{(i,j)} \{|C(i,j)|\} \} \rfloor$$

J. $k_{max}$: maximum spatial scalability level to be reinforced via bitstream

$$(1 \leq k_{max} \leq N +1).$$

K. $b_k$: A sub-bands set in the image decomposed which belong to spatial image resolution level $k$

$$(1 \leq k \leq k_{max}).$$
3.1. The SPIHT Algorithm of Coding

Input: **Quantized** image.

Output: compressed Image File

**SPIHT coding steps:**

**Step 1:** Initialization

\[ n = n_{\text{max}}, \text{ and output } n; \]

\[ LSP_k = 0, \forall K, 1 \leq K \leq K_{\text{max}}; \]

\[ LIP_k = \begin{cases} 0 & \text{for } 1 \leq K < K_{\text{max}} \\ \{(i,j)\}, \forall(i,j) \in H, K=K_{\text{max}} \end{cases} \]

\[ LIS_k = 0, \forall 1 \leq K \leq K_{\text{max}} \}

\[ LIS_{k_{\text{max}}} = f(I,I) \text{ as type A, } \forall(i,j) \in H \text{ that of descendants}; \]

\[ K = K_{\text{max}}. \]

**Step 2:** Sorting pass as resolution-dependent

Sort \( LIP(n,k) \);

Sort \( LIS(n,k) \);

**Step 3:** Refinement pass.

Refine \( LSP(n,k) \);

**Step 4:** Resolution update scale.

If \( k > 1 \) then \( k = k-1 \) and return to step 2;

Else, \( k = k_{\text{max}}. \)

**Step 5:** Quantization-step update.

If \( n > 0 \) then \( n = n-1 \); and back to step 2;

Else, coding end.

**Pseudo code:**

**Sort LIP** \( (k;n) \)

For every entry \((i,j)\) in the \( LIP_k \) output \( Sn(I,j) \);

If \( Sn(I,j) = 1 \), then move \((I,j)\) to the \( LSP_k \), output

\[ C(I,j) \text{ sign}; \]

**Sort LIS** \( (n,k) \)

For each entry \((I,j)\) in the \( LIS_k \)

**RefineLSP** \( (n,k) \)

for every entry \((I,j)\) in the \( LSP_k \), excluding such including in the sorting pass as last (the ones of the same \( n \)), output the \( n'th \) mostly \( c(I,j) \) significant bit.

**Step 6:** Save the result.

**Step 7:** End.

3.2. Statistical Calculations

The function will be used to calculate the quality measurement value as PSNR and MSE. Also, the compression ratio be calculated. The algorithm of this function is as shown below:
Input: Compressed Image and uncompressed image. 
Output: Compression Ratio, PSNR, and MSE values. 
Step 1: Load the Compression Image and uncompressing image. 
Step 2: Apply equations \(2.2\), \(2.6\) and \(2.9\). 
Step 3: display the results. 
Step 4: store the results into the temp file. 
Step 5: End.

4. Implementation of the Suggested System

The suggested system was implementing under windows XP SP2 as operating system environment, and computer Pentium IV with CPU speed 2.4 Gigabyte with RAM of capacity 256 Megabyte. The Flowchart of Suggested System is shown in Figure 4, and Images has size \((256 \times 256)\).

![Flowchart of Suggested System](image)

Figure 4: The block suggested system diagram

5. Results Image Calculations

A somewhat small certain test images selection seems repeatedly in the published reviews on compression of image. Utilizing just some standard images has few profits, i.e., permitting for direct results comparison from diverse compression procedures. Nevertheless, one disadvantage is that the images so-called ”standard” is not essentially standard. For instance, if utilizing a color image with algorithms of gray-scale, how the color image is changed to gray-scale might vary. Likewise, utilizing just some images fails to demonstrate additional generally how a particular algorithm makes on other image types. For instance, some procedures function quite well on the image as House as popular whereas poorly performing on the image as Barbara, and Barbara and House are both ”natural” images examples where compression wavelet-based procedures are recognized to function well. Enactment of diverse multi-wavelet and wavelet procedures significantly changes if ”synthetic” exam images are utilized.
The exam images utilized in the current work were composed from internet various sources. Furthermore, to the mostly commonly utilized natural images[10], a synthetic images number were chosed for obtaining a better overall performance picture of the compression of image procedures. Tables designate that the Multi-wavelets biorthogonal typically offer a higher PSNR compared to other scalar multi-wavelet or wavelet the corresponding values of PSNR are recorded in tables. The bound as upper is shown to be as good as or even better compared to values of PSNR produced via the best multi-wavelets.

<table>
<thead>
<tr>
<th>Image</th>
<th>Filter</th>
<th>C. R</th>
<th>MSE</th>
<th>PSNR(dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>House(256×256)</td>
<td>D4</td>
<td>50.866</td>
<td>0.553</td>
<td>49.796</td>
</tr>
<tr>
<td>GHM</td>
<td>53.571</td>
<td>1.381</td>
<td>51.296</td>
<td></td>
</tr>
<tr>
<td>CL</td>
<td>56.276</td>
<td>1.846</td>
<td>52.796</td>
<td></td>
</tr>
<tr>
<td>ORT4</td>
<td>55.356</td>
<td>1.999</td>
<td>52.286</td>
<td></td>
</tr>
</tbody>
</table>

Table 2: PSNR Results for Barbara

<table>
<thead>
<tr>
<th>Image</th>
<th>Filter</th>
<th>C. R</th>
<th>MSE</th>
<th>PSNR(dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Barbara(256×256)</td>
<td>D4</td>
<td>50.300</td>
<td>0.424</td>
<td>49.226</td>
</tr>
<tr>
<td>GHM</td>
<td>53.005</td>
<td>1.334</td>
<td>50.726</td>
<td></td>
</tr>
<tr>
<td>CL</td>
<td>55.710</td>
<td>1.811</td>
<td>52.226</td>
<td></td>
</tr>
<tr>
<td>ORT4</td>
<td>54.791</td>
<td>1.967</td>
<td>51.716</td>
<td></td>
</tr>
</tbody>
</table>

6. Experimental Results

A Results number in respect to the compression of multi-wavelet and wavelet filters image performance tested might be made according to the results in the current work. First, the multi-wavelets performance of generally relies prominently on the characteristics of image. Regarding images of content of low-frequency mostly (Barbara), wavelets as scalar generally offer performance being good. Nevertheless, multi-wavelets seem excelling at preserving content of high frequency. Particularly, multi-wavelets capture better the edges being sharp and patterns as geometric which happen in the synthetic images as House. Regarding images which have both high and low frequency areas, as several natural images do, generally multi-wavelets with SPIHT offer performance which is in competition to other scalar wavelets.

For some circumstances, i.e., Barbara, multi-wavelets offer better visual quality slightly with similar values of PSNR. Actually, exams on images which contain outsized textured regions (i.e., Barbara) exhibit that multi-wavelets can achieve some of the advantages through high-frequency patterns preserving which are absent by scalar wavelets. Content of high-frequency which is spreading over a outsized image region or that reveals oscillations (i.e., Barbara) is best preserved currently with wavelet generally, but multi-wavelet moderately performs well in few circumstances.

The CL, GHM, and ORT4 multi-wavelets inclined to function best on images being synthetic. Particularly, images of sharp transitions only, i.e., House, are compressed best with either multi-wavelets of ORT4 and CL. It is interestingly to notice that the multi-wavelets as orthogonal, ORT4 and CL nearly show equal performance in most circumstances.
Figure 5: house compressed with ORT4, PSNR = 52.28 dB.
7. Conclusion

In this paper, many conclusions can be drawn according to analysis where results are displayed in section 2.11. Such conclusions are according to 2 gray-scale images (Barbara and House), with different frequency content, compressed with four different multi-wavelet filters bank, with vastly different characteristics. Our conclusions are as follows.

1. Decompositions as multi-wavelet give all traditional wavelets advantages besides the orthogonality combination, symmetry, and short support. The short multi-wavelet filters support bounds ringing artifacts because of consequent quantization. Filter bank symmetry not just pointers to efficient boundary handling, also it conserves mass centers, lessening the fine-scale blurring characters. Orthogonality is beneficial since it worth that rate-distortion optimal strategies quantization might be implemented in the domain transformation and still resulting in optimal quantization of time-domain, as a minimum if fault is measured in a (MSE) sense. Therefore, it is normal to consider the multi-wavelets use in coder as transform-based image.

2. The multi-wavelet transforms method for improving was suggested in the current work, a new decomposition of multi-wavelet which reiterates just on the $L_1$ sub-band, and a method of coefficient shuffling for performance improving with SPIHT based quantizers. Both procedures proved improving the multi-wavelet performance of compression of image in several circumstances. The decomposition iteration improvement uniformly offers better findings and was
thus utilized to produce the findings for all the exam images. Nevertheless, the performance shuffling gains relies upon the content of image to a great extent. Particularly, shuffling aids mostly for images with extra content of low-frequency. Regarding images of extra content of high-frequency, shuffling classically has no important consequence on performance.

3. SPIHT is an image coder multi-wavelet-based compression. It 1st changes the image into its multi-wavelet transformation and then transmits data regarding the wavelet multi-coefficients. The decoder utilizes the signal that received to re-construct the multi-wavelet and functions an inverse transform for recovering the image. The SPIHT and its pre-decessor, the embedded 0 tree wavelet coder, were important advances in still compression of image in that they significantly offered improved quality over JPEG, vector quantization, and wavelets gathered with quantization, while not needing training and producing an embedded bit stream. SPIHT shows exceptional characteristics over many characters all at once include:

- Good image quality with a high PSNR.
- Quick coding and decoding.
- A completely progressive bit-stream.
- Can be utilized for loss-less compression.
- Might be combined with protection of error.
- Capacity for coding for exact bit PSNR or rate.

4. Multi-wavelets have confirmed substantial achievement in still compression of image, with results analogous to wavelet-based compression procedures. It would be a normal extension to endeavor multi-wavelet-based. The new suggested decomposition and SPIHT methods offered in the current work may produce better findings compared to multi-wavelet transform method, in the current work propose utilizing 4-tap Daubechies filter to do compression in the time dimension (such as filtering every pixel at a fixed location of image across succeeding image frames). One of the short multi-wavelet filters, i.e., CL and ORT4 may offer better image quality findings.

References